

The Ph.D. project work ended up with three wonderful conclusions, those are:

(a) Boundedness of the $\bar{\partial}$ -Neumann operator from Sobolev $(-1/2)$ space to Sobolev $(1/2)$ space on domains in which are (i) strongly pseudoconvex with piecewise smooth boundary, (ii) strongly pseudoconvex with Lipschitz boundary. Moreover, the operators, N , $\bar{\partial} N$ and $\bar{\partial}^* N$ are compact on the Sobolev $(-1/2)$ -space.

(b)-existence theorems for the $\bar{\partial}$ -Neumann problem on a strongly $\bar{\partial}$ -convex (Hartogs-pseudoconvex) domain in a Kähler manifold. q

(c) Solutions to the $\bar{\partial}$ -equation with exact support in a domain Ω in a complex manifold X which are (i) strongly $\bar{\partial}$ -convex, (ii) domain with $\bar{\partial}$ -smooth B -regular boundary. $q1C$

3. Concluding remarks

The methodology applied during this program have significant contribution and added more deep insights to the work done by Henkin, Jordan and Kohn, Michel and Shaw, Straube, and others. Similarly, the results in (2) and (3) extend earlier theorems due to Boas and Straube, Chen and Shaw, Derridj, Shaw and also of Cao-Shaw-Wang. In all cases, the techniques used here are fairly standard and well established in the area (exhaustion by smoothly bounded domains, Hörmander's $\bar{\partial}$ -theory, etc), but the technical details are far from trivial and the results obtained certainly represent an important progress in the field